

# Rate of the Bromous Acid–Bromide Reaction Measured in a Br<sub>2</sub>–HOBr Buffer System in Sulfuric Acid Solution

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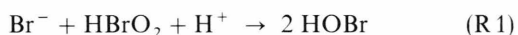
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In the Belousov-Zhabotinsky system bromine species of oxidation states  $-1$  to  $5$  are important for the start and for the inhibition of the autocatalytic reaction steps. Especially, the reaction of  $\text{Br}^-$  with  $\text{HBrO}_2$  competes with the oxidation of  $\text{Ce}^{3+}$  by  $\text{BrO}_2$  formed from  $\text{HBrO}_2$  and  $\text{HBrO}_3$ . In our investigation the reaction of  $\text{Br}^-$  with  $\text{HBrO}_2$  (solvent  $1\text{ M}$  sulfuric acid) is followed spectroscopically in a mixture of bromine and hypobromous acid, which system works as a buffer for bromide. Including experiments on the hydrolysis of  $\text{Br}_2$  and on the solubility product of  $\text{AgBr}$  in  $1\text{ M}$  sulfuric acid solution direct information about the rate constant  $k_1$  of the  $\text{Br}^-/\text{HBrO}_2$  reaction is obtained ( $k_1 = 2.5 \times 10^6\text{ M}^{-2}\text{ s}^{-1}$  at  $20^\circ\text{C}$  and  $4 \times 10^6\text{ M}^{-2}\text{ s}^{-1}$  at  $25^\circ\text{C}$ , which values are valid in the range of  $0.01$  to  $1\text{ M}$  sulfuric acid).

**Key words:** Belousov-Zhabotinsky reaction, Bromous acid, Bromide, Bromine hydrolysis, Bromate, Dual wavelength spectroscopy

## Introduction

In the classical Belousov-Zhabotinsky (BZ) system [1]  $\text{Ce}^{4+}$  is reduced by malonic acid (process 1); the resulting  $\text{Ce}^{3+}$  is oxidized by bromate in several steps starting with a reaction of  $\text{Ce}^{3+}$  with  $\text{BrO}_2$  radicals (process 2 [2, 3]). Process 2 is switched off by species reacting with  $\text{BrO}_2$  directly (like malonyl radicals formed in process 1 [4]) or with  $\text{HBrO}_2$  (like  $\text{Br}^-$  formed in a reaction of  $\text{Ce}^{4+}$  with bromomalonic acid [5, 6]). Process 2 is switched on again as soon as the concentration of the control intermediates is lower than a critical level, and oscillations can occur. For a quantitative understanding of the bromide control information about the rate of the bromide/bromous acid reaction



is needed. The rate of this reaction was investigated first by Noszticzius et al. [7] by following the potential of a bromide sensitive electrode; a rate constant  $1 \times 10^6\text{ M}^{-2}\text{ s}^{-1} < k_1 < 4 \times 10^6\text{ M}^{-2}\text{ s}^{-1}$  was estimated from measurements in  $1.5\text{ M}$  sulfuric acid solution. Aries and Nagy [8] tried to follow this reaction

spectroscopically using stopped flow technique. It turned out that the sensitivity of the method was not high enough to obtain reliable results; nevertheless a value  $k_1 = 1.4 \times 10^6\text{ M}^{-2}\text{ s}^{-1}$  could be roughly estimated from measurements in a reaction medium of  $0.01\text{ M}$  sulfuric acid. They also carried out electrochemical measurements using a bromide sensitive electrode like Noszticzius et al. They found that the reaction rate strongly depended on the acidity of the solution. For  $1\text{ M}$  sulfuric acid solution they obtain  $k_1[\text{H}^+] = 7 \times 10^5\text{ M}^{-1}\text{ s}^{-1}$ . Taking into account thermodynamic data, Field and Försterling [2] proposed a value  $k_1 = 3 \times 10^6\text{ M}^{-2}\text{ s}^{-1}$ .

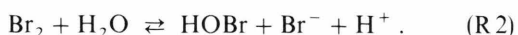
The aim of the present work is to investigate the rate of the  $\text{HBrO}_2\text{--Br}^-$  reaction spectroscopically in a reaction mixture of  $\text{Br}_2$  and  $\text{HOBr}$ . Such a system works as a buffer for bromide; depending on the concentration of  $\text{HOBr}$ , the bromide concentration can be kept extremely low, and the rate of (R 1) can be made small enough to be followed in a conventional kinetic experiment. Such an experiment has already been described by Noszticzius et al. [7]; they used a silverbromide electrode as detecting system. That time it was not clear, however, if a direct reaction of  $\text{Br}_2$  with  $\text{HBrO}_2$  has to be taken into account. In a subsequent work Noszticzius et al. [6] were able to prove that  $\text{HBrO}_2$  is not attacked by bromine directly. That means that the decay of bromine in a  $\text{Br}_2/\text{HBrO}_2$  mixture is exclusively due to a consumption of  $\text{Br}^-$  via (R 1) and that the source of bromide is the hydrolysis

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of bromine:



Similar experiments were carried out by Kshirsagar and Field [9], who measured the formation of HOBr during the reaction of bromate with bromine. As in the experiment of Noszticzius *et al.* [7], bromide is generated during the hydrolysis of bromine, and that bromide reacts directly with bromate,



and with bromous acid, which is formed in (R 3). A second pathway for the disappearance of  $\text{HBrO}_2$  is its disproportionation:



If the set of rate constants for reactions (R 1) to (R 4) from reference [2] is used, it turns out that the calculated rate of formation of HOBr is much higher than observed. In order to fit the calculations to their experiments Kshirsagar and Field assume that the equilibrium constant  $K_2$  of the bromine hydrolysis,

$$K_2 = \frac{[\text{HOBr}][\text{Br}^-][\text{H}^+]}{[\text{Br}_2]}, \quad (1)$$

has to be changed from  $K_2 = 14 \times 10^{-9} \text{ M}^2$  [2] to  $K_2 = 6.6 \times 10^{-10} \text{ M}^2$ . The first value is based on direct measurements by Eigen and Kustin [10] and by Liebhaftsky [11] with corrections for the activities in 1 M sulfuric acid solution calculated by Field, Körös and Noyes [5]. It seems to be strange that these corrections may be wrong by a factor of 20.

Another possibility for the difficulty in explaining the Kshirsagar-Field experiments may be the uncertainty in the value of the rate constant  $k_1$ . If that value is really lower than assumed in their calculations the overall rate of HOBr formation is expected to be lower too. This was already mentioned by Försterling and Schreiber [12].

## Experiments

### Chemicals

$\text{H}_2\text{SO}_4$  (96%), NaBr,  $\text{AgNO}_3$  and  $\text{Ag}_2\text{SO}_4$  (all Fluka pa.) were used without further purification.  $\text{NaBrO}_3$  was recrystallized twice from hot water.  $\text{NaBrO}_2$  was prepared following the procedure of Noszticzius *et al.* [7]. Solutions of HOBr in water were prepared using a method described by Betts and

Mackenzie [13];  $\text{Ag}_2\text{SO}_4$  was added to a solution of bromine in water, the precipitate of AgBr was removed by filtration and the remaining solution was purified by vacuum distillation at about 30°C.

The concentration of the aqueous HOBr solutions was calculated from the absorbance peak at 263 nm using  $\epsilon(\text{HOBr}) = 90 \text{ M}^{-1} \text{ cm}^{-1}$ . That value was derived from a separate experiment in which HOBr was injected into 0.1 M NaOH solution; the concentration of NaOBr formed this way was calculated from its absorbance at 330 nm using the well known value  $\epsilon(\text{NaOBr}) = 303 \text{ M}^{-1} \text{ cm}^{-1}$  at 330 nm reported by Lee and Lister [14].  $\epsilon(\text{HOBr})$  at 263 nm was found to be the same within 2% in 1 M  $\text{H}_2\text{SO}_4$  and in water. For comparison,  $\epsilon(\text{HOBr}) = 87 \text{ M}^{-1} \text{ cm}^{-1}$  at 265 nm is reported for a solution of HOBr in 1.66 M  $\text{HClO}_4$  [13].

The concentration of the alkaline  $\text{NaBrO}_2$  solutions was determined spectroscopically using the extinction coefficients reported by Lee and Lister [14]. From the ratio of the absorbances at 296 and 330 nm the contamination of  $\text{NaBrO}_2$  by NaOBr was estimated to be less than 2%. If an  $\text{NaBrO}_2$  solution was injected into 1 M sulfuric acid, a small amount of bromine was formed due to a reaction of traces of bromide with excess  $\text{HBrO}_2$ ; from this measurement a 3% contamination of the  $\text{NaBrO}_2$  stock solution by bromide was estimated.

Traces of bromine in sulfuric acid solutions of  $\text{NaBrO}_3$  were removed by bubbling nitrogen gas through the solution; the remaining solution was checked spectroscopically for traces of HOBr impurities. All solutions were prepared from doubly distilled water.

### Evaluation of experimental data and numerical methods

The analog signal of the measuring system was digitized by a 12 bit analog-digital converter, and the data were stored and evaluated in the memory of an Apple II computer connected with a Taxan plotter. The numerical integration of the kinetic differential equations was performed with the program DIFFGL, which is based on Gear's method [15], by using an IBM PS/2 personal computer.

### Equilibrium constant $K_2$

For the evaluation of the kinetic data in the experiments presented here a reliable value of the equilib-

rium constant  $K_2$  of the bromine hydrolysis reaction (R2) in 1 M sulfuric acid medium is needed. The equilibrium concentration of bromide formed by the hydrolysis of  $\text{Br}_2$  was measured by titration of the solution with  $\text{Ag}^+$ ; the end point was detected by measuring the light scattering of  $\text{AgBr}$  particles in equilibrium with silver and bromide ions:



$$L_{\text{AgBr}} = [\text{Ag}^+][\text{Br}^-] \quad (2)$$

( $L_{\text{AgBr}}$  = solubility product of silverbromide). This way the equilibrium concentration of bromide in the bromine solution can be calculated according to

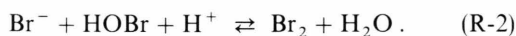
$$[\text{Br}^-] = L_{\text{AgBr}}/[\text{Ag}^+]_{\text{p}} \quad (3)$$

if  $[\text{Ag}^+]_{\text{p}}$  is the concentration of added silver ions needed for the first appearance of  $\text{AgBr}$  precipitate.

Since the solubility product of  $\text{AgBr}$  will be different in 1 M sulfuric acid solution compared to neutral solution and no data in literature were available, the change of  $L_{\text{AgBr}}$  from neutral to acidic solution was measured first. In the actual procedure a  $1 \times 10^{-3}$  M solution of  $\text{AgNO}_3$  in water was added in small aliquots to 140 ml of a  $1 \times 10^{-6}$  M  $\text{Br}^-$  solution in water; the sample cell (optical pathlength 10.7 cm) was illuminated by a tungsten lamp, and the absorbance  $A$  was recorded at a wavelength of 401 nm using a dual wavelength apparatus (reference wavelength 601 nm) as described earlier [16]. As soon as the concentration  $[\text{Ag}^+]_{\text{p}}$  was reached, the absorbance of the solution increased rapidly, as can be seen in Fig. 1 (curve 1). From  $[\text{Ag}^+]_{\text{p}} = 1 \times 10^{-6}$  M and  $[\text{Br}^-] = 1 \times 10^{-6}$  M the solubility product  $L_{\text{AgBr}} = 1 \times 10^{-12} \text{ M}^2$  was calculated according to (3). Additional data result in a mean value  $L_{\text{AgBr}} = (1.0 \pm 0.1) \times 10^{-12} \text{ M}^2$  at a temperature of 22 °C.

The same procedure was applied with bromide and silver ions solved in 1 M  $\text{H}_2\text{SO}_4$ . From the experiment displayed in Figure 1 (curve 2) and from additional data the value  $L_{\text{AgBr}} = (2.3 \pm 0.2) \times 10^{-12} \text{ M}^2$  is obtained. That means that  $L_{\text{AgBr}}$  is higher in 1 M sulfuric acid solution by a factor of about 2 compared to a solution in water.

In order to measure the equilibrium constant  $K_2$ , a solution of bromine was prepared by mixing hypobromous acid and bromide,



By such a procedure a much purer product was obtained compared to the direct dissolution of elemen-

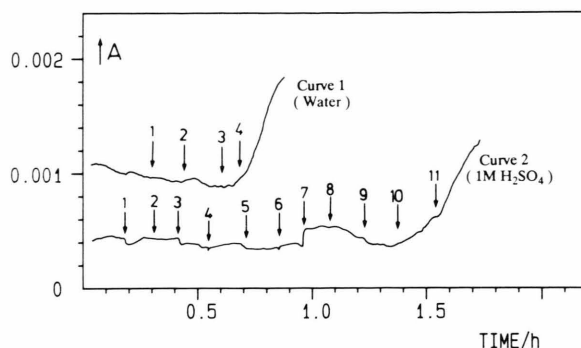


Fig. 1. Titration experiment in the  $\text{Br}^-$ -system at 22 °C. Dual wavelength technique, wavelength 401 nm, reference wavelength 601 nm, optical pathlength 10.7 cm. Absorbance  $A$  of 140 ml of a  $1 \times 10^{-6}$  M  $\text{NaBr}$  solution as a function of time during the addition of small aliquots of a  $1 \times 10^{-3}$  M  $\text{AgNO}_3$  solution. – Curve 1:  $\text{NaBr}$  solved in water; at points 1, 2, 3, 4 the volumes of added  $\text{AgNO}_3$  solution were 50, 50, 20, 20  $\mu\text{l}$ . The total volume of added solution is 0.140 ml, hence  $[\text{Ag}^+]_{\text{p}} = 1 \times 10^{-6}$  M and  $L_{\text{AgBr}} = 1 \times 10^{-12} \text{ M}^2$ . – Curve 2:  $\text{NaBr}$  solved in 1 M  $\text{H}_2\text{SO}_4$ ; at points 1, 2, ..., 11 the volumes of added  $\text{AgNO}_3$  solution were 50, 50, 50, 30, 20, 20, 20, 20, 20, 20, 20  $\mu\text{l}$ . The total volume of added solution is 0.320 ml, hence  $[\text{Ag}^+]_{\text{p}} = 2.3 \times 10^{-6}$  M and  $L_{\text{AgBr}} = 2.3 \times 10^{-12} \text{ M}^2$ .

tary bromine in 1 M sulfuric acid, which solution was not stable for a longer time.  $\text{Ag}^+$  was added until the increase of absorbance indicated the end point of the titration. In the actual procedure 1.12 ml of a 0.01 M  $\text{NaBr}$  solution were added into 140 ml of a  $1.5 \times 10^{-4}$  M  $\text{HOBr}$  solution in 1 M sulfuric acid. The resulting  $\text{Br}_2$  and  $\text{HOBr}$  initial concentrations were  $[\text{Br}_2] = 0.80 \times 10^{-4}$  M and  $[\text{HOBr}] = (1.50 - 0.80) \times 10^{-4} \text{ M} = 0.70 \times 10^{-4}$  M. The concentration of bromine was checked spectroscopically by its absorbance at 401 nm.

After that, the  $\text{Br}_2$  absorbance was balanced and the absorbance  $A$  of the solution was followed at a much higher sensitivity in order to see the increase of absorbance due to the light scattering of  $\text{AgBr}$  particles. It turned out that in this case the best results were obtained with a single beam technique at a wavelength of 601 nm (instead of the dual wavelength technique used in the experiments described above). A 0.1 M solution of  $\text{AgNO}_3$  was added in small aliquots, and the sharp increase of absorbance due to the light scattering of  $\text{AgBr}$  particles was observed (Figure 2). As a result,  $[\text{Ag}^+]_{\text{p}} = 2.50 \times 10^{-4}$  M is obtained, and the bromide concentration is calculated according to (3) using the solubility product of  $\text{AgBr}$  determined above for 1 M sulfuric acid solution:  $[\text{Br}^-] = 9.20 \times 10^{-9}$  M.

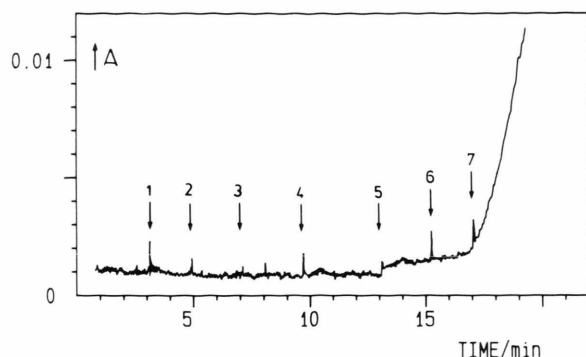


Fig. 2. Titration experiment in the  $\text{Br}_2/\text{HOBr}$ -system at  $22^\circ\text{C}$ . Single beam technique, wavelength 601 nm, optical path length 10.7 cm, 1 M sulfuric acid as solvent. – Absorbance  $A$  of a  $8.0 \times 10^{-5}$  M bromine solution (prepared by injection of 1.12 ml of a 0.01 M  $\text{NaBr}$  solution into 140 ml of a  $1.50 \times 10^{-4}$  M  $\text{HOBr}$  solution) as a function of time during the addition of  $\text{AgNO}_3$ . At points 1 to 7 equal volumes of 50  $\mu\text{l}$  of a 0.1 M  $\text{AgNO}_3$  solution were added. The total volume added is 0.35 ml, hence  $[\text{Ag}^+]_p = 2.50 \times 10^{-4}$  M.

Now  $K_2$  is calculated according to (1) with  $[\text{H}^+] = 1.29$  M, the concentration of  $\text{H}^+$  in 1 M sulfuric acid [17]:

$$K_2 = (9.20 \times 10^{-9} - 7.0 \times 10^{-5} \cdot 1.29/0.80 \times 10^{-4}) \text{ M}^2 \\ = 10.4 \times 10^{-9} \text{ M}^2.$$

The results of a series of similar experiments are collected in Table 1; from these experiments a mean value  $K_2 = (11 \pm 1) \times 10^{-9} \text{ M}^2$  is obtained for a medium of 1 M sulfuric acid at a temperature of  $22^\circ\text{C}$ .

#### Kinetic measurements

In order to follow the reaction of  $\text{HBrO}_2$  with  $\text{Br}^-$  in a bromine buffer solution, a bromine solution in 1 M sulfuric acid was prepared from excess  $\text{HOBr}$  and  $\text{Br}^-$  as described above and thermostated at  $25^\circ\text{C}$ ; in a typical experiment the bromine and  $\text{HOBr}$  initial concentrations were  $[\text{Br}_2] = 1 \times 10^{-4}$  M and  $[\text{HOBr}] = 2.0 \times 10^{-5}$  M. Into 140 ml of that solution 1.0 ml of a  $7.0 \times 10^{-4}$  M  $\text{NaBrO}_2$  solution was injected, leading to a  $\text{HBrO}_2$  initial concentration of  $5.0 \times 10^{-6}$  M. The  $\text{NaBrO}_2$  was solved in a mixture of 0.01 M  $\text{NaOH}$  and 0.5 M  $\text{Na}_2\text{SO}_4$ , which solution has nearly the same index of refraction as 1 M sulfuric acid; this way Schlieren effects during the injection, which might disturb the measurement of the small absorbance changes significantly, could be avoided. The change  $\Delta A$  of the absorbance due to the decay of bromine was followed using the dual wavelength technique (optical

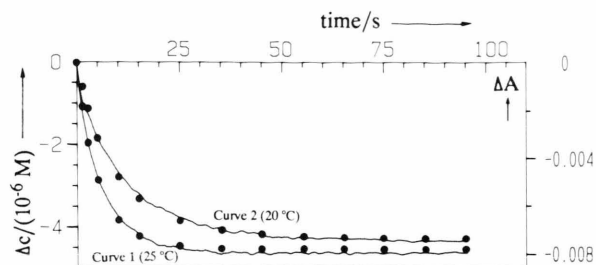


Fig. 3. Change of the absorbance  $\Delta A$  (right hand scale) during the reaction of  $\text{HBrO}_2$  (initial concentration  $5 \times 10^{-6}$  M) with  $\text{Br}_2$  (initial concentration  $1 \times 10^{-4}$  M) in 1 M sulfuric acid solution containing  $\text{HOBr}$  (initial concentration  $2 \times 10^{-5}$  M). Curve 1:  $25^\circ\text{C}$ , curve 2:  $20^\circ\text{C}$ . The change  $\Delta c$  of the bromine concentration (left hand scale) was calculated as explained in the text. The experiments are compared to theory (dots) using the rate constants summarized in Table 2 ( $[\text{H}^+] = 1.29$  M for 1 M sulfuric acid solution).

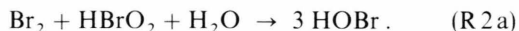
Table 1. Evaluation of the equilibrium constant  $K_2$ ; the way of calculation is demonstrated in the text using run 11 as an example.

Run	$[\text{HOBr}]$ $10^{-5}$ M	$[\text{Br}_2]$ $10^{-5}$ M	$[\text{Ag}^+]_p$ $10^{-4}$ M	$[\text{Br}^-]$ $10^{-9}$ M	$K_2$ $10^{-9}$ M
1	7.1	1.0	17.14	1.34	12.3
2	7.1	2.0	7.86	2.93	13.4
3	8.0	2.9	7.86	2.93	10.6
4	8.0	2.9	7.50	3.07	11.1
5	7.2	4.0	5.00	4.60	10.6
6	7.1	5.1	3.57	6.44	11.6
7	7.1	5.0	4.29	5.37	9.7
8	7.0	6.0	3.21	7.16	10.8
9	7.0	7.0	2.50	9.20	11.8
10	6.9	7.0	2.50	9.20	11.6
11	7.0	8.0	2.50	9.20	10.4
12	7.0	9.0	2.14	10.7	10.7
13	9.1	10.0	2.14	10.7	12.6
14	9.1	10.0	2.50	9.20	10.7

path length 10.7 cm, sample wavelength 401 nm, reference wavelength 601 nm); the result is displayed in Figure 3 (curve 1, right hand scale). It should be mentioned that even in the absence of added  $\text{HBrO}_2$  a slow linear decrease of the absorbance  $A$  was observed, which is attributed to a slow decay of the bromine concentration. Within 100 s the decay was  $\Delta A = 0.0004$ , that is about 5% of the final absorbance change in Figure 3. The curves displayed in Figure 3 (and also in the following figures) are corrected for this small decay. The decay is less than 0.2% of the initial bromine concentration, hence no correction for this value is needed.

For comparison, the same experiment was repeated at a temperature of  $20^\circ\text{C}$  (Fig. 3, curve 2). From the

change  $\Delta A$  of the absorbance we obtain the change  $\Delta c$  of the bromine concentration in the following way. If we combine (R 1) and (R 2) we find for the stoichiometry of the overall reaction of bromine with bromite



That means that for each bromine molecule which disappears three HOBr molecules are formed. Hence

$$\begin{aligned} \Delta A &= d [\varepsilon(\text{Br}_2) \Delta c - \varepsilon(\text{HOBr}) 3 \Delta c] \\ &= d \Delta c [\varepsilon(\text{Br}_2) - 3 \varepsilon(\text{HOBr})] \end{aligned} \quad (4)$$

From the absorption spectra of  $\text{Br}_2$  and HOBr we obtain the extinction coefficients  $\varepsilon(\text{Br}_2) = 172 \text{ M}^{-1} \text{ cm}^{-1}$  and  $\varepsilon(\text{HOBr}) = 4 \text{ M}^{-1} \text{ cm}^{-1}$  at  $\lambda = 401 \text{ nm}$ ; the optical path length  $d$  used in the experiments was  $d = 10.7 \text{ cm}$ . This way the change  $\Delta c$  of the bromine concentration was calculated (Fig. 3, left hand scale). The final values of  $\Delta c$  are  $-4.6 \times 10^{-6}$  and  $-4.3 \times 10^{-6} \text{ M}$  at 25 and 20°C, respectively. The expected values for exclusive reaction of  $\text{HBrO}_2$  with  $\text{Br}^-$  are  $5 \times 10^{-6} \text{ M}$  in both cases. That means that only a small fraction of  $\text{HBrO}_2$  disappears via the disproportionation reaction (R 4). This fraction is larger at 20°C compared to 25°C due to the smaller reaction rate of (R 1).

Additional measurements were performed with the same bromine concentration, but the initial concentration of HOBr was changed in the range from  $2 \times 10^{-5} \text{ M}$  to  $2 \times 10^{-4} \text{ M}$  (Fig. 4a, curves 1–4). By increasing the HOBr concentration the equilibrium (R 2) is shifted to the left hand side, and this way the rate of reaction (R 1) is slowed down. This can be clearly seen in the experiments; as a consequence, the disproportionation reaction becomes more and more important, and the final value  $\Delta c$  moves far away from the theoretical  $5 \times 10^{-6} \text{ M}$  value.

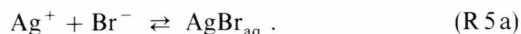
In a third set of experiments, a 1 : 1 ratio of the bromine and HOBr initial concentrations was applied, but the absolute bromine concentration was changed by a factor of 20 from  $1 \times 10^{-4} \text{ M}$  to  $5 \times 10^{-6} \text{ M}$  (Figure 5a). The rate of bromine consumption decreases with decreasing initial concentrations.

## Discussion

### Equilibrium (R 2)

First we have to discuss the results obtained for  $L_{\text{AgBr}}$  and for  $K_2$ . The solubility product of AgBr in water was carefully measured at different tempera-

tures by Gledhill and Malan [18] using a precise conductivity method; the value  $5.08 \times 10^{-13} \text{ M}^2$  was obtained at 25°C. The value  $1.0 \times 10^{-12} \text{ M}^2$  found in our experiment in water solution is higher by a factor of 2. Apparently, this discrepancy must be due to some systematic error in the method used by us. One possibility might be that part of the AgBr formed during (R 5) in the experiment does not precipitate, but remains solved as  $\text{AgBr}_{\text{aq}}$ :



Hence the amount of added  $\text{Ag}^+$  at the first appearance of light scattering is larger than the amount required to exceed the solubility product. The equilibrium (R 5a) was investigated by Berne and Leden [19] using tracer methods. They report the value  $K_{\text{sa}} = 1.4 \times 10^4 \text{ M}^{-1}$  at an ionic strength of 0.1 M (established by  $\text{NaClO}_4$ ). Pulse radiolysis measurements performed by Schmidt *et al.* and by Meisel [20] lead to a value  $K_{\text{sa}} = 3 \times 10^4 \text{ M}^{-1}$  in  $1 \times 10^{-4} \text{ M HClO}_4$ . From (R 5a) we derive

$$[\text{AgBr}_{\text{aq}}] = K_{\text{sa}} [\text{Ag}^+] [\text{Br}^-] = K_{\text{sa}} L_{\text{AgBr}} \quad (5)$$

Even with the highest values of  $K_{\text{sa}}$  and of  $L_{\text{AgBr}}$  the concentration of solved AgBr does not exceed  $6 \times 10^{-8} \text{ M}$ , that is less than 4% of the concentration of silver and bromide in the ionic state. Hence the discrepancy in our determination of the solubility product cannot be explained this way, unless supersaturation of the solution is taken into account.

It was not our aim, however, to measure an absolute value of  $L_{\text{AgBr}}$ , but to see the change, if the solvent water is replaced by the solvent 1 M sulfuric acid; in this case the systematic error should be very similar in both determinations. It turns out that  $L_{\text{AgBr}}$  is higher by a factor of 2.3 in 1 M sulfuric acid compared to a solution in water. Following the arguments of Field, Körös, and Noyes [5] concerning the activity coefficients in 1 M  $\text{H}_2\text{SO}_4$ , we have to write down the equation for the solubility product  $L^*$  of AgBr in terms of activities  $a$ :

$$(L_{\text{AgBr}})^* = a_{\text{Ag}^+} a_{\text{Br}^-} = f^2 [\text{Ag}^+] [\text{Br}^-] = f^2 L_{\text{AgBr}} \quad (6)$$

In water as a solvent the activity coefficients  $f$  are unity; if these activity coefficients are set equal to 0.7 for 1 M  $\text{H}_2\text{SO}_4$  solution as proposed in [5], the solubility product is expected to be higher in 1 M sulfuric acid by a factor of two compared to a solution in water; this is nearly what we find in our experiment. A similar result was obtained by Berne and Leden

[19]; they find an increase of the solubility product of AgBr by a factor of 1.7 if the ionic strength is increased from 0 to 0.1 M (NaClO<sub>4</sub> solution).

In the bromine/HOBr experiment the amount of added silver ions up to the first appearance of light scattering will also be higher than expected for the first appearance of AgBr precipitate. In order to calculate the bromide concentration in equilibrium with bromide and HOBr it seems to be reasonable to use the value  $L_{\text{AgBr}} = 2.3 \times 10^{-12} \text{ M}^2$  of the solubility product as determined in our experiments described above. This way the value  $K_2 = 11 \times 10^{-9} \text{ M}^2$  was found for 1 M sulfuric acid solution at a temperature of 22 °C. The values  $5.8 \times 10^{-9} \text{ M}^2$  and  $8.3 \times 10^{-9} \text{ M}^2$  are reported by Liebhafsky [11] for the neutral solution at 25 and 30 °C, respectively. For better comparison we have to recalculate our value for these temperatures. We assume the validity of the thermodynamic relation between the equilibrium constant  $K_2$  and the change of Gibb's energy  $\Delta G^0$  in the standard state:

$$\ln(K_2/\text{M}^2) = -\Delta G^0/(RT). \quad (7)$$

According to (7) our value  $K_2 = 11 \times 10^{-9} \text{ M}^2$  changes into  $K_2 = 10 \times 10^{-9} \text{ M}^2$  and  $13 \times 10^{-9} \text{ M}^2$ , if we change the temperature from 22 °C to 20 °C and 25 °C, respectively; these values are higher by a factor of 2 compared to the corresponding Liebhafsky values.

If the same estimation of the activity coefficients is applied in the case of the hydrolysis reaction (R 2), we find for the hydrolysis constant  $(K_2)^*$  in terms of activities

$$(K_2)^* = a_{\text{HOBr}} a_{\text{Br}^-} a_{\text{H}^+} / a_{\text{Br}_2} = f^2 K_2. \quad (8)$$

With  $f = 0.7$  for charged species in 1 M sulfuric acid solution [5]  $K_2$  is expected to be larger by a factor of 2, just as obtained in our experiment.

In our opinion there is no doubt that  $K_2$  increases from water as solvent to 1 M sulfuric acid by a factor of two as already calculated by Field, Körös, and Noyes [5]. The assumption of Kshirsagar and Field [9] that  $K_2$  decreases by a factor of 20 is completely in disagreement with our experiments.

#### Bromide/bromite reaction in a bromine buffer system

First we discuss the experiments displayed in Figure 3. In this case the disproportionation reaction (R 4) is of minor importance for the kinetics compared to reactions (R 1) and (R 2). Since the value of the

equilibrium constant  $K_2$  is well established now we are able to deduce a rate constant for reaction (R 1). Since the HOBr concentration increases during the reaction, it is not possible to evaluate  $k_1$  by an analytical procedure. Instead of this we performed numerical calculations treating  $k_1$  as a parameter. From  $K_2 = 13 \times 10^{-9} \text{ M}^2$  and the Eigen-Kustin value  $k_{-2} = 8 \times 10^9 \text{ M}^{-2} \text{ s}^{-1}$  [10] we deduce  $k_2 = K_2 k_{-2} = 104 \text{ s}^{-1}$  at 25 °C. The rate constant for the disproportionation of  $\text{HBrO}_2$  is  $k_4 = 3000 \text{ M}^{-1} \text{ s}^{-1}$  at 20 °C [2]. Similar measurements as described in [2] were carried out at 30 °C leading to  $k_4 = 4000 \text{ M}^{-1} \text{ s}^{-1}$ ; interpolation for 25 °C gives  $k_4 = 3500 \text{ M}^{-1} \text{ s}^{-1}$ . The calculations were done with  $[\text{H}^+] = 1.29 \text{ M}$  corresponding to 1 M sulfuric acid solution [17]. The best fit for curve 1 in Fig. 3 was obtained with  $k_1 = 4 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  (Fig. 3, dots).

In the case of the 20 °C experiment  $k_2 = 80 \text{ s}^{-1}$  is obtained from  $K_2 = 10 \times 10^{-9} \text{ M}^2$  and  $k_{-2} = 8 \times 10^9 \text{ M}^{-2} \text{ s}^{-1}$ . With  $k_4 = 3000 \text{ M}^{-1} \text{ s}^{-1}$  the best fit of curve 2 in Fig. 3 is achieved with  $k_1 = 2.5 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  (Fig. 3, dots).

The rate constants used in these calculations are summarized in Table 2. The value  $k_1 = 2.5 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  determined from our experiments at 20 °C is in good agreement with the value  $3 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  reported by Field and Försterling [2]; it is larger, however, by a factor of 6 than the value  $0.4 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  deduced for 20 °C from the Ariese and Nagy value  $k_1 [\text{H}^+] = 0.7 \times 10^6 \text{ M}^{-1} \text{ s}^{-1}$  [8] (with  $[\text{H}^+] = 1.29 \text{ M}$  and assuming the same temperature dependence as in our experiment) obtained from electrochemical measurements. With the same set of rate constants the kinetics of the curves in Figs. 4 a and 5 a are calculated and displayed in Figs. 4 b and 5 b. The main features of the experimental curves are very well modelled in the calculations. Systematic deviations occur in the final state of the reaction only, when the disproportionation of  $\text{HBrO}_2$  becomes important (curves 2–4 in Figure 4). In these cases the experimental curves are higher in the final state than the calculated ones by about 20% indicating that the disproportionation of  $\text{HBrO}_2$  is faster than assumed for a second order reaction. Such a behavior was already observed in the reaction of  $\text{HBrO}_2$  with bromate if  $\text{HBrO}_2$  is applied at concentrations lower than  $3 \times 10^{-6} \text{ M}$  [2].

More information from Figs. 3 to 5 is obtained by comparing the initial slopes of the experimental curves to theory. In this case the disproportionation of  $\text{HBrO}_2$ , the decay of bromine and the increase of

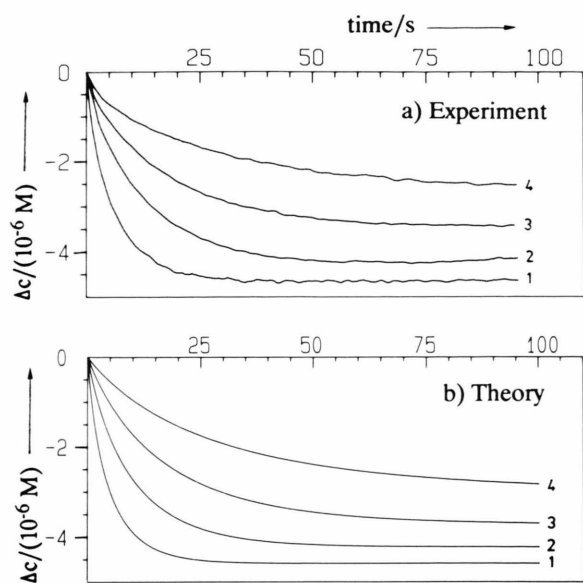


Fig. 4. Experiment as described in Fig. 3 at 25°C with  $[\text{Br}_2] = 1 \times 10^{-4} \text{ M}$  and different HOBr-concentrations:  $2 \times 10^{-5} \text{ M}$  (curve 1),  $5 \times 10^{-5} \text{ M}$  (curve 2),  $1 \times 10^{-4} \text{ M}$  (curve 3),  $2 \times 10^{-4} \text{ M}$  (curve 4). a) experimental curves (25°C), b) calculated curves (rate constants from Table 2, 25°C,  $[\text{H}^+] = 1.29 \text{ M}$  for 1 M sulfuric acid solution).

HOBr can be neglected. We only need equations (R 1) and (R 2) to calculate the initial slopes. Assuming a steady state for the bromide ions we find

$$[\text{Br}^-]_{\text{stat}} = k_2 [\text{Br}_2] / (k_{-2} [\text{HOBr}] [\text{H}^+] + k_1 [\text{HBrO}_2] [\text{H}^+]). \quad (9)$$

With the rate constants in Table 2,  $[\text{H}^+] = 1.29 \text{ M}$ ,  $[\text{HOBr}] > 5 \times 10^{-6} \text{ M}$  and  $[\text{HBrO}_2] = 5 \times 10^{-6} \text{ M}$  we find that the second term in the denominator of (9) can be completely neglected under the conditions of our experiments:

$$[\text{Br}^-]_{\text{stat}} = K_2 \frac{[\text{Br}_2]}{[\text{HOBr}] [\text{H}^+]}. \quad (10)$$

The stationary bromide concentration depends on the ratio of the bromine and HOBr concentrations only and not on their absolute values. That means the system works as a buffer for bromide similar as a pH buffer solution works as a buffer for  $\text{H}^+$ . The rate of bromine consumption is equal to the rate of consumption of  $\text{HBrO}_2$  via (R 1):

$$\begin{aligned} \frac{d[\text{Br}_2]}{dt} &= \frac{d[\text{HBrO}_2]}{dt} = -k_1 [\text{Br}^-]_{\text{stat}} [\text{HBrO}_2] [\text{H}^+] \\ &= -k_1 K_2 [\text{HBrO}_2] [\text{Br}_2] / [\text{HOBr}]. \end{aligned} \quad (11)$$

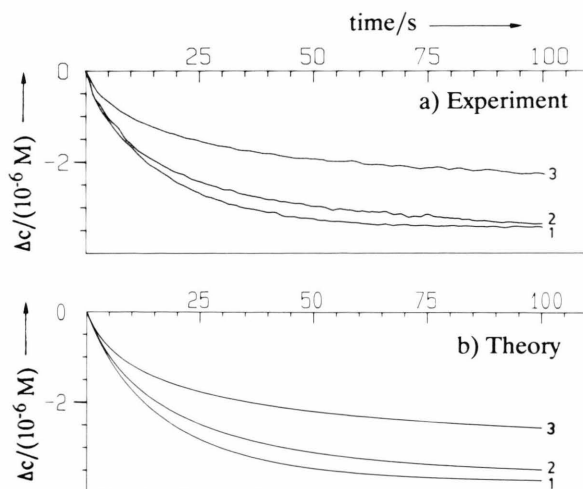


Fig. 5. Experiment as described in Fig. 3 at 25°C with the ratio  $[\text{Br}_2] : [\text{HOBr}] = 1 : 1$  at different HOBr- and  $\text{Br}_2$  concentrations:  $1 \times 10^{-4} \text{ M}$  (curve 1),  $2 \times 10^{-5} \text{ M}$  (curve 2),  $5 \times 10^{-6} \text{ M}$  (curve 3). a) experimental curves (25°C), b) calculated curves (rate constants from Table 2, 25°C,  $[\text{H}^+] = 1.29 \text{ M}$  for 1 M sulfuric acid solution).

Table 2. Rate constants  $k_1$  to  $k_4$  and equilibrium constant  $K_2$  used in the calculations at 20 and 25°C. a) Value determined here, b) value determined in [2].

Constants	$T = 20^\circ\text{C}$	$T = 25^\circ\text{C}$	Source
$k_1 / (\text{M}^{-2} \text{s}^{-1})$	$2.5 \times 10^6$	$4 \times 10^6$	a)
$k_{-1} / (\text{M}^{-1} \text{s}^{-1})$	$2 \times 10^{-5}$	$2 \times 10^{-5}$	b)
$k_2 (\text{s}^{-1})$	$0.8 \times 10^2$	$1.04 \times 10^2$	a)
$k_{-2} / (\text{M}^{-2} \text{s}^{-1})$	$8 \times 10^9$	$8 \times 10^9$	b)
$k_3 / (\text{M}^{-2} \text{s}^{-1})$	1.6		a)
$k_{-3} / (\text{M}^{-1} \text{s}^{-1})$	3.2	3.2	b)
$k_4 / (\text{M}^{-1} \text{s}^{-1})$	$3 \times 10^3$	$3.5 \times 10^3$	a), b)
$k_{-4} / (\text{M}^{-1} \text{s}^{-1})$	$1 \times 10^{-8}$	$1 \times 10^{-8}$	b)
$K_2 / (\text{M}^2)$	$10 \times 10^{-9}$	$13 \times 10^{-9}$	a)

Table 3. Initial slopes  $d[\text{Br}_2]/dt$  of the experimental and theoretical curves displayed in Figs. 4–5 (initial concentrations  $[\text{Br}_2]_0$  and  $[\text{HOBr}]_0$ ). The theoretical values are calculated from (11), rate constant  $k_1$  and equilibrium constant  $K_2$  see Table 2 (25°C), initial concentration of  $\text{HBrO}_2$  is  $5 \times 10^{-6} \text{ M}$ .

Curve	$[\text{Br}_2]_0$ $10^{-6} \text{ M}$	$[\text{HOBr}]_0$ $10^{-6} \text{ M}$	$(d[\text{Br}_2]/dt)_{t=0}$ $10^{-6} \text{ M}$	
			Exper.	Theory
1 (Fig. 4)	100	20	1.3	1.30
2 (Fig. 4)	100	50	0.46	0.52
3 (Fig. 4)	100	100	0.30	0.26
4 (Fig. 4)	100	200	0.20	0.13
2 (Fig. 5)	20	20	0.30	0.26
3 (Fig. 5)	5	5	0.30	0.26

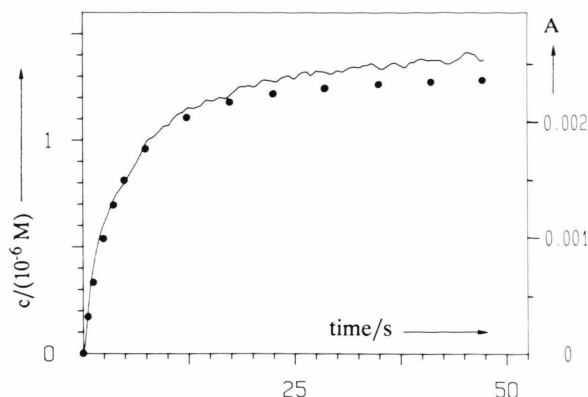


Fig. 6. Formation of  $\text{Br}_2$  during the reaction of  $\text{Br}^-$  (initial concentration  $3 \times 10^{-6} \text{ M}$ ) with  $\text{HBrO}_2$  (initial concentration  $1 \times 10^{-6} \text{ M}$ ) in  $0.01 \text{ M}$  sulfuric acid solution at  $25^\circ\text{C}$ . Solid line: experimental curve. Right hand scale: absorbance  $A$  at  $401 \text{ nm}$ . Left hand scale: concentration  $c$  of  $\text{Br}_2$  obtained from  $A$  with optical path length  $d = 10.7 \text{ cm}$  and  $\varepsilon(\text{Br}_2) = 172 \text{ l mol}^{-1} \text{ cm}^{-1}$ . The dots are calculated bromine concentrations ( $k_1$ ,  $k_{-1}$ ,  $k_{-2}$ , and  $k_4$  see Table 2,  $k_2 = 46 \text{ s}^{-1}$  according to the equilibrium constant  $K_2 = 5.8 \times 10^{-9} \text{ M}^2$  valid in diluted sulfuric acid solution,  $[\text{H}^+] = 0.016 \text{ M}$ ).

It should be noted that the rate of consumption of bromine is expected to be independent of  $[\text{H}^+]$ . For the experiments displayed in Figs. 3–5 the experimental initial slopes  $d[\text{Br}_2]/dt$  and the slopes calculated from (11) (with initial concentrations  $[\text{HBrO}_2]_0$ ,  $[\text{Br}_2]_0$ , and  $[\text{HOBr}]_0$ ) are compared in Table 3. It turns out that theory and experiment agree very well. Especially, the initial slopes of the curves in Fig. 5 are equal as predicted by theory (due to the same ratio  $[\text{Br}_2]_0 : [\text{HOBr}]_0 = 1 : 1$ ).

#### Direct reaction of bromide and bromite in $0.01 \text{ M}$ sulfuric acid

Although the results obtained in our experiments with bromine as a buffer for bromide ions are well consistent with the set of rate constants listed in Table 2, a direct experiment on (R 1) would be very helpful. From the electrochemical experiments of Ariese and Nagy [8] it is clear that reaction (R 1) cannot be followed directly at high sulfuric acid concentration. For this reason we performed an experiment in  $0.01 \text{ M}$  sulfuric acid solution at  $25^\circ\text{C}$ . Into  $140 \text{ ml}$  of a  $3 \times 10^{-6} \text{ M}$  solution of  $\text{NaBr}$  in  $0.01 \text{ M}$   $\text{H}_2\text{SO}_4$   $875 \mu\text{l}$  of a  $1.6 \times 10^{-4} \text{ M}$   $\text{NaBrO}_2$  solution were injected, resulting in an initial concentration  $[\text{HBrO}_2]_0 = 1 \times 10^{-6} \text{ M}$ . According to the 3 : 1 ratio of bromide and bromite a second order decay of bromide is ex-

pected; the final concentration of bromine formed during the reaction should be  $2 \times 10^{-6} \text{ M}$ . In the actual experiment displayed in Fig. 6 a fast rise of the absorbance  $A$  is observed, which leads to a final absorbance  $A = 0.0026$  corresponding to a final bromine concentration  $0.0026/(10.7 \times 172) \text{ M} = 1.4 \times 10^{-6} \text{ M}$ . This is 30% less than expected for complete reaction of  $\text{Br}^-$  with  $\text{HBrO}_2$ . In this experiment the initial  $\text{HBrO}_2$  concentration is lower by a factor of 5 compared to the  $\text{HBrO}_2$  concentrations used in the former experiments; it is most improbable that the low yield of bromine is due to the disproportionation of bromous acid. On the other hand, we see from (1) that the fraction of bromide and hypobromous acid in equilibrium with bromine increases with decreasing  $\text{H}^+$  concentration and with decreasing bromine initial concentration. In fact, the sulfuric acid concentration in our experiment is lower by a factor of 100 and the bromine concentration is lower by a factor of 2.5 compared to curve 3 in Figure 5. From (1) we calculate for the concentration of bromide formed by hydrolysis of bromine (initial concentration  $c_0$ ):

$$[\text{Br}^-] = -K_2/(2[\text{H}^+]) + \sqrt{K_2 c_0/[\text{H}^+] + (K_2/(2[\text{H}^+]))^2}. \quad (12)$$

In [17] the concentration  $[\text{H}^+]$  of sulfuric acid is listed down to  $[\text{H}_2\text{SO}_4] = 0.1 \text{ M}$ ; in this case  $[\text{H}^+] = 0.138 \text{ M}$  is reported. Additional data [21] are available for  $[\text{H}_2\text{SO}_4] = 0.005 \text{ M}$ ; from the measured  $\text{pH} = 2.1$  we calculate  $[\text{H}^+] = 0.008 \text{ M}$  if we assume that there is no significant difference between activity and concentration. From this value we estimate  $[\text{H}^+] = 0.016 \text{ M}$  at  $[\text{H}_2\text{SO}_4] = 0.01 \text{ M}$ . On the other hand, for  $0.01 \text{ M}$  sulfuric acid medium the original Liebhafsky value  $5.8 \times 10^{-9} \text{ M}^2$  should be better suited than our value  $13 \times 10^{-9} \text{ M}^2$  derived for  $1 \text{ M}$  sulfuric acid solution. Inserting  $c_0 = 2 \times 10^{-6} \text{ M}$ ,  $[\text{H}^+] = 0.016 \text{ M}$  and  $K_2 = 5.8 \times 10^{-9} \text{ M}^2$  into (12) we obtain  $[\text{Br}^-] = 0.7 \times 10^{-6} \text{ M}$ . That means that 35% of the bromine disappears, and the final concentration  $[\text{Br}_2] = 1.3 \times 10^{-6} \text{ M}$  is expected, which value is near to the measured  $1.4 \times 10^{-6} \text{ M}$ . The calculated kinetics of the formation of bromine is compared to experiment in Figure 6 (dots). Regarding the uncertainties in our assumptions on  $K_2$  and on  $[\text{H}^+]$ , experiment and theory agree well.

In the Ariese/Nagy experiments [8] a value  $k_1[\text{H}^+] = 3 \times 10^4 \text{ M}^{-1} \text{ s}^{-1}$  is given for  $0.02 \text{ M}$   $\text{H}_2\text{SO}_4$ ; our experiment is modelled well by  $k_1[\text{H}^+] = 4 \times 10^6$

$0.016 = 6.4 \times 10^4 \text{ M}^{-1} \text{ s}^{-1}$ ; that value should be higher by a factor of two for 0.02 M sulfuric acid solution. This result indicates that in this case the  $k_1$  value determined by electrochemical measurements is too low by a factor of about 4. We repeated the electrochemical experiments of Ariese and Nagy [8] at a sulfuric acid concentration of 0.01 M; within the limits of error the same result for  $k_1$  as reported in [8] was obtained if the same way of evaluation of the experimental data was applied. From this point of view the results of the electrochemical method seem to be reliable. In our opinion, however, there is a systematic error in the interpretation of the experimental data. At  $[\text{H}_2\text{SO}_4] = 0.01 \text{ M}$  and bromide concentration of about  $1 \times 10^{-6} \text{ M}$  the hydrolysis of  $\text{Br}_2$  is significantly shifted to the bromide side just as in our experiment displayed in Figure 6. That means that the bromide concentration decreases from an initial value  $c_0$  to a value  $c_x$ , which is about 30% of  $c_0$  instead of zero as assumed in the evaluation by Ariese and Nagy. If that real  $c_x$  value would be used in the calculation, a significantly larger  $k_1$  would be expected. The same argument is valid for higher sulfuric acid concentrations, since in these cases  $[\text{Br}^-]_0$  was further reduced in order to decrease the rise time in the kinetic experiment. Moreover, the spectroscopic experiment performed by Ariese and Nagy [8] results in  $k_1 = 1.4 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$ , which value is larger by a factor of two compared to their electrochemical experiments. In this case the initial bromide concentration was about 2 orders larger than in the electrochemical experiments;  $[\text{Br}^-]_x$  is less than 1% of the initial concentration, and the evaluation of the data is correct in this case.  $k_1$  obtained this way is still too low compared to our value by a factor 3, possibly due to problems with imperfect mixing during the stopped flow experiment as already mentioned by the authors.

#### Reaction of bromine with bromate

Nevertheless the difficulties in explaining the low reaction rate during the reaction of bromine with excess bromate as reported by Kshirsagar and Field [9] are not yet resolved. On the basis of the experimental results presented here severe changes of  $K_2$  as proposed in [9] cannot be justified. In order to obtain additional experimental data, we reexamined that reaction by using lower initial concentrations of bromine and by using a more sensitive method of detection. In our experiment 2 ml of a  $8.8 \times 10^{-3} \text{ M}$

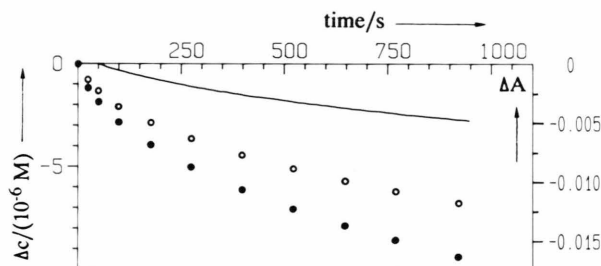


Fig. 7. Decay of bromine (initial concentration  $5 \times 10^{-5} \text{ M}$ ) in the reaction with bromate (0.1 M) in 1 M sulfuric acid at  $20^\circ\text{C}$ . Solid line: experiment. The registration starts 50 s after the addition of NaBr. Right hand scale: change  $\Delta A$  of the absorbance at 401 nm (dual wavelength method, reference 601 nm). Left hand scale: change  $\Delta c$  of the bromine concentration calculated from  $\Delta A$  as described in the text. Dots and circles: Theory. The dots are calculated on the basis of the  $20^\circ\text{C}$  rate constants listed in Table 2 ( $[\text{H}^+] = 1.29 \text{ M}$ ); the circles are calculated with  $k_1 = 0$  (Reaction (R1) neglected).

NaBr solution were added to 210 ml of a 0.1 M solution of  $\text{NaBrO}_3$  in 1 M sulfuric acid at  $20^\circ\text{C}$ . This way an initial concentration of  $[\text{Br}_2] = 5 \times 10^{-5} \text{ M}$  was obtained. The change  $\Delta A$  of the absorbance at 401 nm (measured by the dual wavelength method, reference wavelength 601 nm) is displayed in Figure 7 (solid line); the registration of  $\Delta A$  starts 50 s after the addition of NaBr. From  $\Delta A$  the change  $\Delta c$  of bromine is calculated using a relation similar to (4); from the overall reaction



we conclude that 5 HOBr molecules are formed for two disappearing bromine molecules and the factor 3 in (4) has to be changed into 2.5.  $\Delta c$  was calculated using the  $20^\circ\text{C}$  rate constants in Table 2.  $k_3 = 1.6 \text{ M}^{-2} \text{ s}^{-1}$  as measured by Lamberz [22] was preferred instead of the  $2.5 \text{ M}^{-2} \text{ s}^{-1}$  value given in [9], since the first value was obtained with bromate in excess as in the current experiment. The calculated curve is compared to experiment in Figure 7 (Dots). As in the Kshirsagar/Field experiment, the rate of bromine disappearance turns out to be smaller by a factor of about 3 compared to the calculations. In order to estimate the contribution of (R1) a second calculation with  $k_1 = 0$  was performed (Fig. 7, circles). In this case only one half of the bromine should disappear; nevertheless, the final value of  $\Delta c$  is reduced by less than 30% only. The reason is that in this case the HOBr production rate is smaller too and the hydrolysis reaction (R2) is shifted more to the right hand

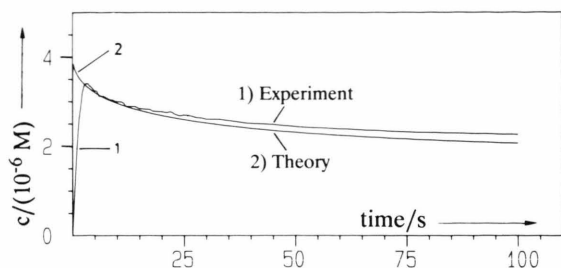


Fig. 8. Formation and decay of bromine during the reaction of bromide (initial concentration  $5 \times 10^{-6}$  M) with bromite (initial concentration  $5 \times 10^{-6}$  M) at  $20^\circ\text{C}$  in 1 M sulfuric acid. Curve 1: experiment. The concentration  $c$  of bromine was calculated from the absorbance  $A$ ; as in Figs. 3–5 the contribution of  $\text{HOBr}$  to  $A$  was taken into account. Curve 2: Theory. The calculation was started with an initial concentration  $6 \times 10^{-6}$  M of  $\text{Br}^-$  in order to obtain the same initial concentration of bromine as observed in the experiment. The rate constants used in the calculation are the  $20^\circ\text{C}$  values in Table 2 ( $[\text{H}^+] = 1.29$  M).

side. That means that reasonable changes in  $k_1$  do not lead to significant changes in the overall reaction rate. Of course, it would be possible to model the experiment by assuming a  $K_2$  value which is lower by a factor of 10 as proposed in [9]. In this case, however,  $k_1 = 25 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  would be needed according to (11) to explain our experiment displayed in Figure 3; such a high value would be inconsistent with the direct experiment shown in Figure 6. Another possibility would be to decrease  $k_3$  from  $1.6 \text{ M}^{-2} \text{ s}^{-1}$  to  $0.16 \text{ M}^{-2} \text{ s}^{-1}$  although this rate constant seems to be well established. It should be mentioned, however, that  $k_3$  was measured with  $1 \times 10^{-4}$  M bromide solutions [22]; the bromide concentration in the actual experiment is lower by about two orders of magnitude. Moreover it is known that bromate in sulfuric acid solution is unstable;  $\text{HOBr}$  is formed slowly, which might shift the equilibrium (R 2) more to the left hand side than assumed. Anyway, additional experiments are required to solve the problem.

#### Bromide/bromite reaction with excess $\text{HBrO}_2$

The reaction of bromide with bromite in competition with silver ions was investigated by Försterling and Schreiber [12]. In these experiments  $\text{HBrO}_2$  and  $\text{NaBr}$  solutions of equal concentrations were injected into 1 M sulfuric acid solution. A fast rise of the absorbance due to the formation of bromine is observed. After that process, excess  $\text{HBrO}_2$  reacts with bromide, which is in equilibrium with bromine according to (1),

and part of the bromine disappears (see Fig. 5a in [12]). In order to model the kinetics of the bromine decay it was necessary to use  $k_1 [\text{H}^+] = 5 \times 10^5 \text{ M}^{-1} \text{ s}^{-1}$ , which value is even less than the Ariese/Nagy value. According to the results obtained in the present investigation, such a procedure cannot be justified. For this reason the experiment was repeated, and the result was compared to calculations using the set of rate constants listed in Table 2. A typical run is displayed in Figure 8. Into 140 ml of a solution of  $5 \times 10^{-6}$  M  $\text{NaBr}$  in 1 M sulfuric acid thermostated at  $20^\circ\text{C}$  840  $\mu\text{l}$  of a  $8.4 \times 10^{-4}$  M solution of  $\text{NaBrO}_2$  were injected, leading to a  $\text{HBrO}_2$  initial concentration  $5 \times 10^{-6}$  M. From the overall reaction



a maximum bromine concentration of  $3.3 \times 10^{-6}$  M is expected; after that starting reaction an excess of  $3.3 \times 10^{-6}$  M  $\text{HBrO}_2$  is present in the solution. Unfortunately, the maximum value of the experimental curve is reached not before 3 s due to the process of mixing and the rise time of the apparatus. The maximum value corresponds to a concentration of  $3.3 \times 10^{-6}$  M as expected, the zero time value, however, is larger and can be roughly extrapolated as  $3.9 \times 10^{-6}$  M, which value is higher by 18%. Part of this discrepancy can be attributed to some bromide and hypobromite impurities in the  $\text{NaBrO}_2$  sample, but this way we cannot account for the whole effect. Anyway, a simulation of the kinetics has to start with that high value of bromide initial concentration. Using the set of rate constants valid for  $20^\circ\text{C}$  and starting with a bromide initial concentration of  $6 \times 10^{-6}$  M (which value leads to  $3.9 \times 10^{-6}$  M bromine as obtained in the experiment) and a bromite initial concentration of  $5 \times 10^{-6}$  M, the calculated curve in Fig. 8 is obtained. Experiment and theory agree well, although the final bromine concentration is higher in the experiment; as already discussed in connection with Figs. 4 and 5, this may be due to a faster disproportionation process of  $\text{HBrO}_2$  than expected for a clear second order reaction. We conclude that the high value of  $k_1$  derived in the present work is compatible with this last experiment and that there is no need to use a lower value in the calculations. Of course, the conclusions drawn in [12] will be changed if a higher  $k_1$  value is introduced. For example, the effective rate of bromide removal by silver ions will be increased by a factor of 5. These implications will be discussed separately.

## Conclusions

We have proved that the bromine hydrolysis equilibrium (R 2) is shifted from water to 1 M sulfuric acid as solvent in practically the same way as originally predicted by Field, Körös, and Noyes [5]. There is a small difference between the Eigen and Kustin value  $K_2 = 6.9 \times 10^{-9} \text{ M}^2$  (20 °C, ionic strength 0.1 M) [10] and the Liebhafsky value  $K_2 = 4.2 \times 10^{-9} \text{ M}^2$  (extrapolated from the 25 °C value  $5.8 \times 10^{-9} \text{ M}^2$  to 20 °C, ionic strength 0) [11], which is most probably due to the change in ionic strength (the factor of 1.6 is practically the same as in the case of the solubility product of AgBr reported in [19]). We prefer the Liebhafsky value, because it is directly obtained from equilibrium experiments, and results at different temperatures are available. In our actual kinetic calculations we have maintained  $k_{-2} = 8 \times 10^9 \text{ M}^{-2} \text{ s}^{-1}$  [2];  $k_2$  was derived from  $K_2$  and  $k_{-2}$  as can be seen from Table 2. This way  $k_2 = 110 \text{ s}^{-1}$  as given in [5] has to be changed into  $80 \text{ s}^{-1}$  (20 °C) and  $104 \text{ s}^{-1}$  (25 °C). Perhaps it would be more reasonable to maintain  $k_2$  and to adjust  $k_{-2}$ , but the results of our calculations depend on  $K_2$  only and not at all on any arbitrary splitting into  $k_2$  and  $k_{-2}$  provided that  $k_{-2}$  is in the order of  $10^9 \text{ M}^{-2} \text{ s}^{-1}$ .

From our direct measurements at  $[\text{H}_2\text{SO}_4] = 0.01 \text{ M}$ , and from our more indirect measurements in bromine buffer systems at  $[\text{H}_2\text{SO}_4] = 1 \text{ M}$ , consistent values of the rate constant  $k_1$  at 20 °C and 25 °C are derived. Our values  $k_1 = 2.5 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  (at 20 °C) and  $k_1 = 4 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  (at 25 °C) are larger by a factor of 6 compared to the rate constants obtained by

Ariese and Nagy [8] from electrochemical measurements at different  $\text{H}_2\text{SO}_4$  concentrations; on the other hand, our 20 °C value is very near to  $3 \times 10^6 \text{ M}^{-2} \text{ s}^{-1}$  as proposed in [2] on the basis of thermodynamic data on (R 1).

The unexpected low rate of the bromine-bromate reaction, as pointed out first by Kshirsagar and Field [9], could be proved in an independent experiment. An explanation of that discrepancy seems to be difficult, and further work is needed. Anyway, it can be excluded that the equilibrium (R 2) is much more shifted to the left hand side than assumed so far.

The result obtained with the reaction of excess bromite with bromide has implications on the conclusions drawn from a competition experiment with added silver ions [12], [23]. That competition experiment was modelled with the low  $k_1$  value predicted in [8]; but it is clear now that the interpretation is also consistent with the high  $k_1$  value established in the present investigation. One consequence will be that the rate constant for effective removal of bromide by silver ions has to be increased from  $3 \times 10^4 \text{ M}^{-1} \text{ s}^{-1}$  to  $1.5 \times 10^5 \text{ M}^{-1} \text{ s}^{-1}$ .

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